

PHYSICS 534

EXERCISE-17

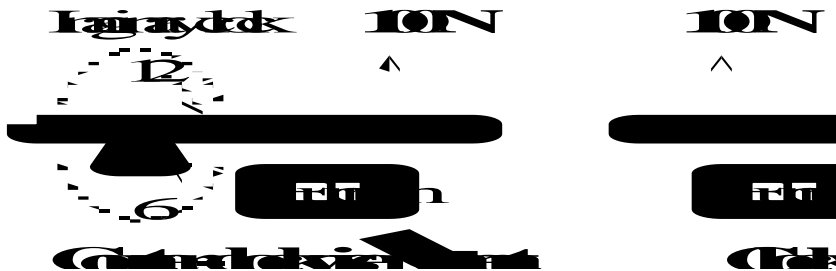
Moments



Heike Onnes was awarded the Nobel prize for physics in 1913 for his investigations into matter at very low temperatures.



The moment of a force (also known as the torque) is the tendency of the force to produce rotation. The point about which rotation takes place is called the *fulcrum*. By definition, a fulcrum is an *immovable* reference point usually designated by a solid triangle (\blacktriangle). The rotation of a moment is specified as either clock-wise or counter-clock-wise with reference to the fulcrum. Study the diagram below illustrating a force producing a counter-clockwise moment and clockwise moment. Note that the point of application of the force (left or right of the fulcrum) determines the rotation (clock-wise or counter-clock wise) of the moment.



The formula for the moment of a force is:

$$M = Fd_{\perp}$$

where: M is the moment (in newton-meters)

F is the force (in newtons)

d_{\perp} is the perpendicular distance from the force to the fulcrum (in meters)

The Law of Moments says that:

“When a system is in equilibrium, the *sum* of all the moments rotating a system clockwise equals the *sum* of all the moments rotating the system counter-clock wise.” Or, mathematically:

$$\Sigma \text{ clockwise moments} = \Sigma \text{ counter-clockwise moments}$$

or

$$\Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

↳ **Important:** Whenever a system is in equilibrium, the Law of Moments applies about any fulcrum (point) in the system regardless of the location of the fulcrum.

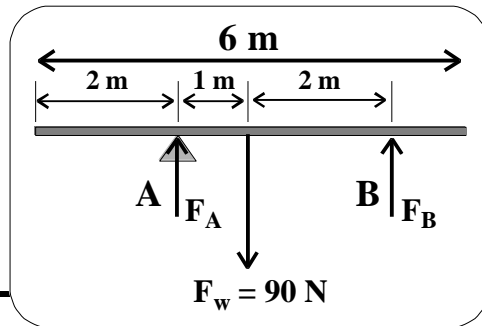


1. Define in your own words "the moment of a force".

The tendency of a force to produce rotation.



2. Two men, A and B, support a *uniform* plank on their shoulders. The plank is 6 m long and has a mass of 9 kg. Calculate how much of the weight each man carries if the plank extends 2 m beyond A's shoulder and 1 m beyond B's shoulder. [60 N] [30 N]



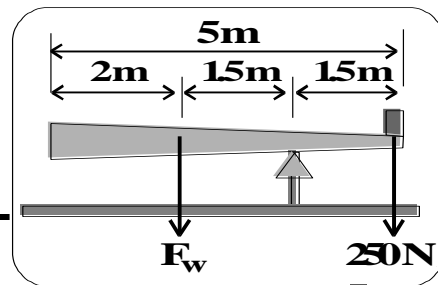
Take moments at point A.

$$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

$$(90 \text{ N})(1 \text{ m}) = F_B (3 \text{ m}) \quad \text{or} \quad F_B = \frac{(90 \text{ N})(1 \text{ m})}{3 \text{ m}} = 30 \text{ N}$$

$$\therefore F_A = 90 \text{ N} - 30 \text{ N} = 60 \text{ N}$$

3. A *tapered* plank which is 5 m long has its center of gravity 2 m from the thick end. It is balanced horizontally on a block 1.5 m from the thin end when a weight of 250 N is placed at the thin end. What is the weight of the plank? [250 N]



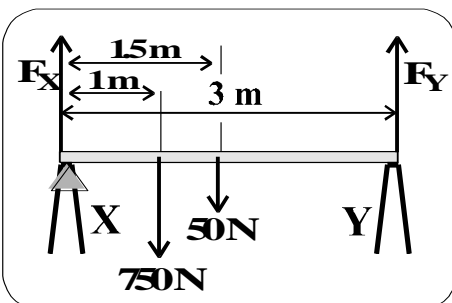
Take moments about point of balance.

$$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

$$\therefore (250 \text{ N})(1.5 \text{ m}) = F_w (1.5 \text{ m})$$

$$F_w = \frac{(250 \text{ N})(1.5 \text{ m})}{1.5 \text{ m}} = 250 \text{ N}$$

4. A worker weighing 750 N stands on a *uniform* plank 3 m long that is supported by two step-ladders X and Y. The plank weighs 50 N. If the worker stands 1 m from one end of the plank, what force is supported by each step ladder. [525 N] [275 N]



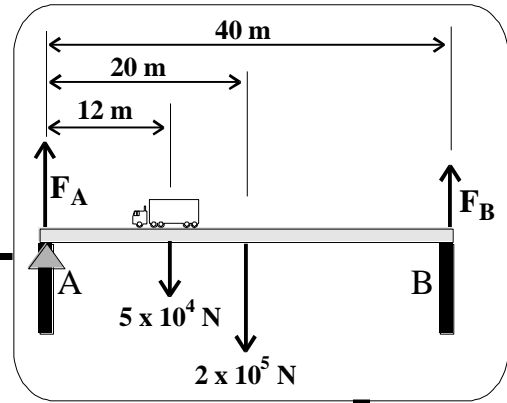
Take moments about point X.

$$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

$$\therefore (750 \text{ N})(1 \text{ m}) + (50 \text{ N})(1.5 \text{ m}) = F_Y (3 \text{ m})$$

$$F_Y = \frac{825 \text{ N} \cdot \text{m}}{3 \text{ m}} = 275 \text{ N} \quad \therefore F_X = 800 \text{ N} - 275 \text{ N} = 525 \text{ N}$$

5. A bridge is supported by two columns, A and B. The bridge is 40 m long and weighs $2 \times 10^5 \text{ N}$. A truck weighing $5 \times 10^4 \text{ N}$ is 12 m from column-A. Calculate the upward force exerted by each column. [$1.35 \times 10^5 \text{ N}$] [$1.15 \times 10^5 \text{ N}$]



Take moments about point A.

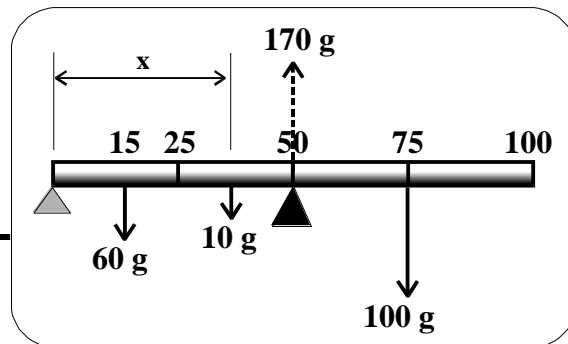
$$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

$$\therefore (5 \times 10^4 \text{ N})(12 \text{ m}) + (2 \times 10^5 \text{ N})(20 \text{ m}) = F_B(40 \text{ m})$$

$$F_B = \frac{(5 \times 10^4 \text{ N})(12 \text{ m}) + (2 \times 10^5 \text{ N})(20 \text{ m})}{40 \text{ m}} = 1.15 \times 10^5 \text{ N}$$

$$F_A = 2.5 \times 10^5 \text{ N} - 1.15 \times 10^5 \text{ N} = 1.35 \times 10^5 \text{ N}$$

6. A uniform meter stick is supported at its center. A load of 60 g hangs at the 15 cm point and a load of 100 g hangs at the 75 cm mark. Where should a 10 g mass be hung so as to produce equilibrium? [10 cm]



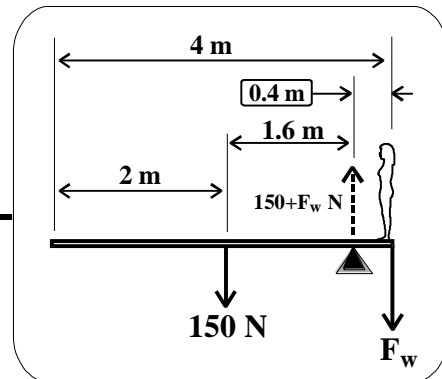
Take moments from the zero point and treat the grams as forces.

$$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

$$\therefore (60 \text{ g})(15 \text{ cm}) + (10 \text{ g})(x) + (100 \text{ g})(75 \text{ cm}) = (170 \text{ g})(50 \text{ cm})$$

$$x = \frac{(170 \text{ g})(50 \text{ cm}) - (60 \text{ g})(15 \text{ cm}) - (100 \text{ g})(75 \text{ cm})}{10 \text{ g}} = 10 \text{ cm}$$

7. A *uniform* plank 4 m long has a mass of 15 kg. A girl finds that the plank will balance if supported by a fulcrum 40 cm from *her* end. Find the weight of the girl. [600 N]



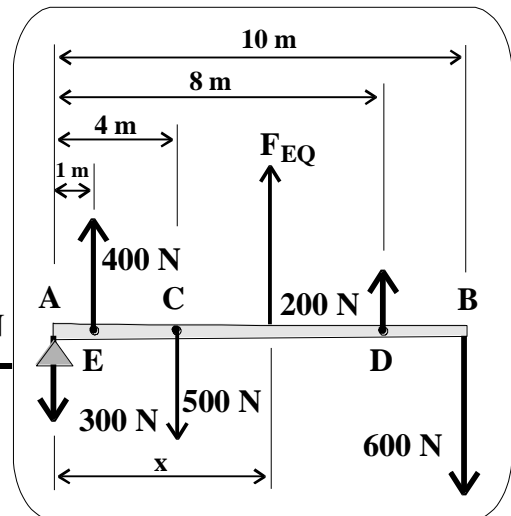
Take moments about the point of balance.

$$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$$

$$(F_w)(0.4 \text{ m}) = (150 \text{ N})(1.6 \text{ m})$$

$$\therefore F_w = \frac{(150 \text{ N})(1.6 \text{ m})}{0.4 \text{ m}} = 600 \text{ N}$$

8. A plank, AB, is 10 m long and has a mass of 50 kg. Its center of gravity, C, is 4 m from end A. At A, a force of 300 N acts downward. At end B, a force of 600 N acts downward. At D, 2 m from end B, a force of 200 N acts upward. At E, 1 m from end A, a force of 400 N acts upward. Find:



- ❶ The force required to produce equilibrium. [800 N]

Since the system is at rest, $F_R = 0$

$\therefore \Sigma \text{ Forces up} = \Sigma \text{ Forces down}$

$$400 \text{ N} + F_{EQ} + 200 \text{ N} = 300 \text{ N} + 500 \text{ N} + 600 \text{ N}$$

$$\therefore F_{EQ} = 800 \text{ N North}$$

- ❷ The point of application of the equilibrant force (from end-A): [7.5 m]

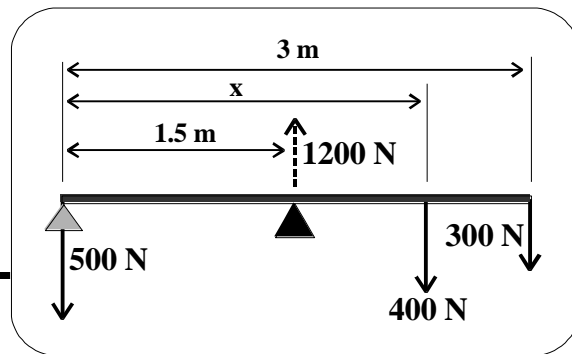
Take moments about point A.

$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$

$$\therefore (500 \text{ N})(4 \text{ m}) + (600 \text{ N})(10 \text{ m}) = (400)(1 \text{ m}) + (800 \text{ N})(x) + (200 \text{ N})(8 \text{ m})$$

$$(800 \text{ N})x = 2800 \text{ N} \cdot \text{m} \quad \therefore x = \frac{2800 \text{ N} \cdot \text{m}}{800 \text{ N}} = 7.5 \text{ m}$$

9. A 30 kg boy and a 50 kg boy sit at opposite ends of a 3 m long seesaw which is pivoted at its center. Where must a 40 kg boy sit, from the 50 kg boy, in order to balance the seesaw? [2.25 m]



Take moments about the 500 N boy.

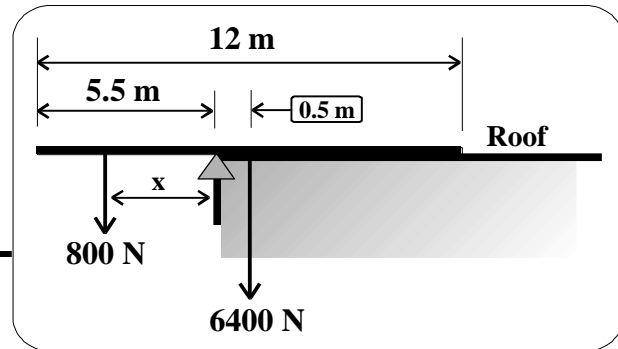
$\therefore \Sigma \text{ cwm} = \Sigma \text{ ccwm}$

$$(400 \text{ N})(x) + (300 \text{ N})(3 \text{ m}) = (1200 \text{ N})(1.5 \text{ m})$$

$$\therefore (400 \text{ N})(x) = (1200 \text{ N})(1.5 \text{ m}) - (300 \text{ N})(3 \text{ m})$$

$$x = \frac{(1200 \text{ N})(1.5 \text{ m}) - (300 \text{ N})(3 \text{ m})}{400 \text{ N}} = \frac{900 \text{ N} \cdot \text{m}}{400 \text{ N}} = 2.25 \text{ m}$$

10. A 640 kg iron beam, 12 m long, rests on the roof of a building such that one end overhangs the roof by 5.5 m. How far *from the roof* can an 80 kg man walk out on the beam without falling? [4 m]



Take moments from edge of roof.

$$\therefore \sum \text{cwm} = \sum \text{ccwm}$$

$$\therefore (6400 \text{ N})(0.5 \text{ m}) = (800 \text{ N})(x)$$

$$x = \frac{(6400 \text{ N})(0.5 \text{ m})}{(800 \text{ N})} = 4 \text{ m}$$

